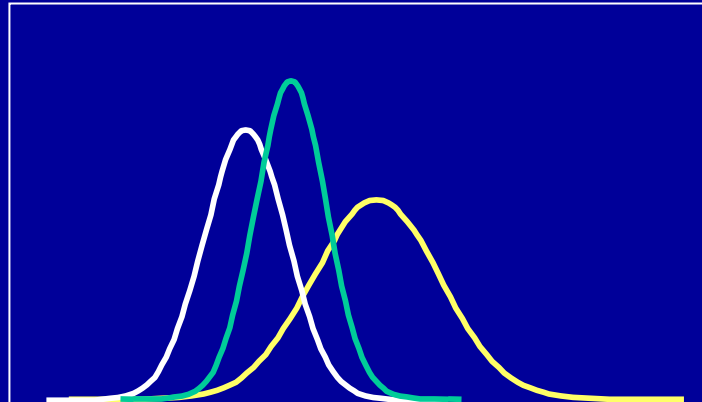


US EPA ARCHIVE DOCUMENT

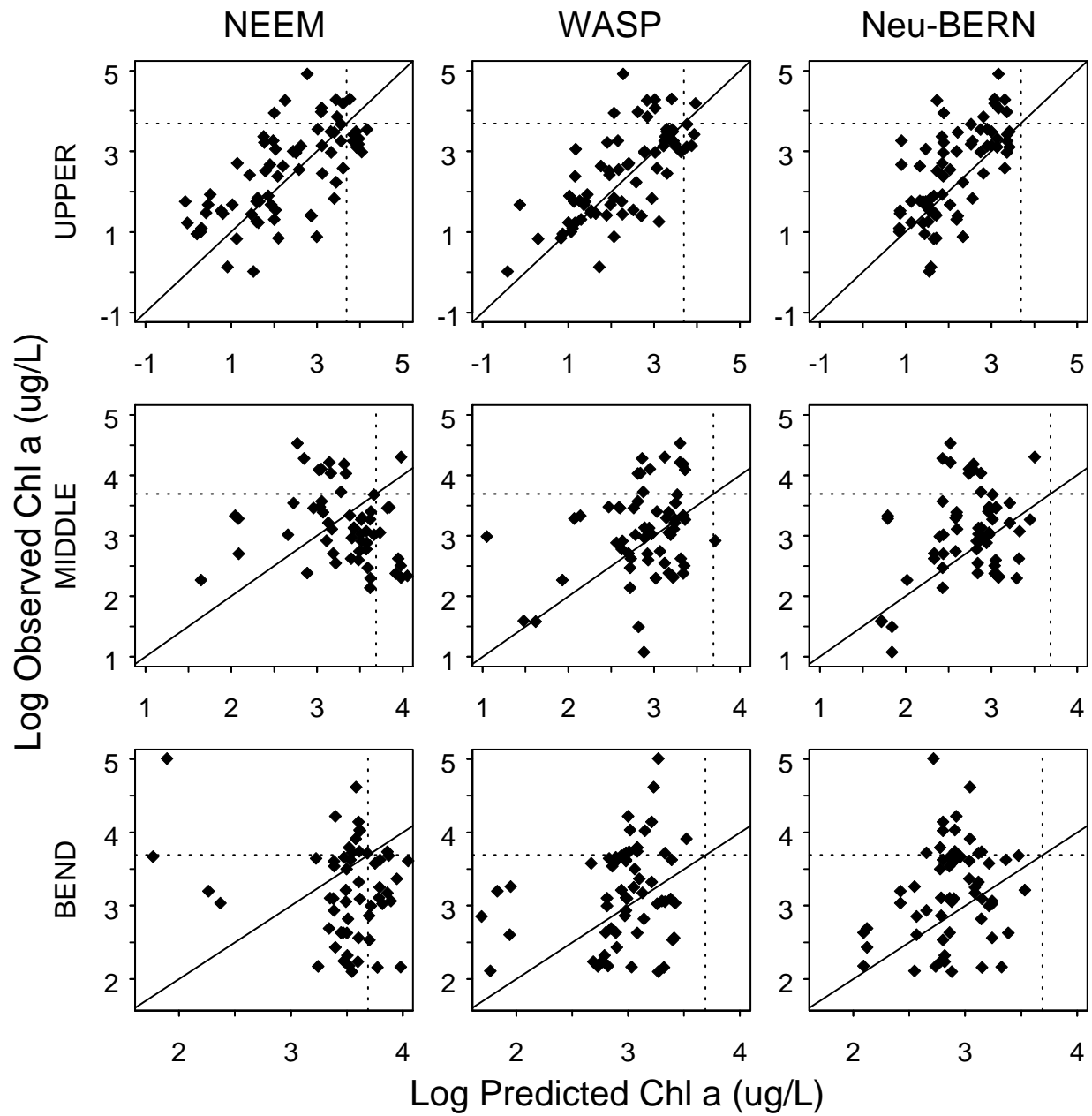
# Adaptive Implementation Modeling and Monitoring for TMDL Refinement

K.H. Reckhow  
Duke University  
November 3, 2005

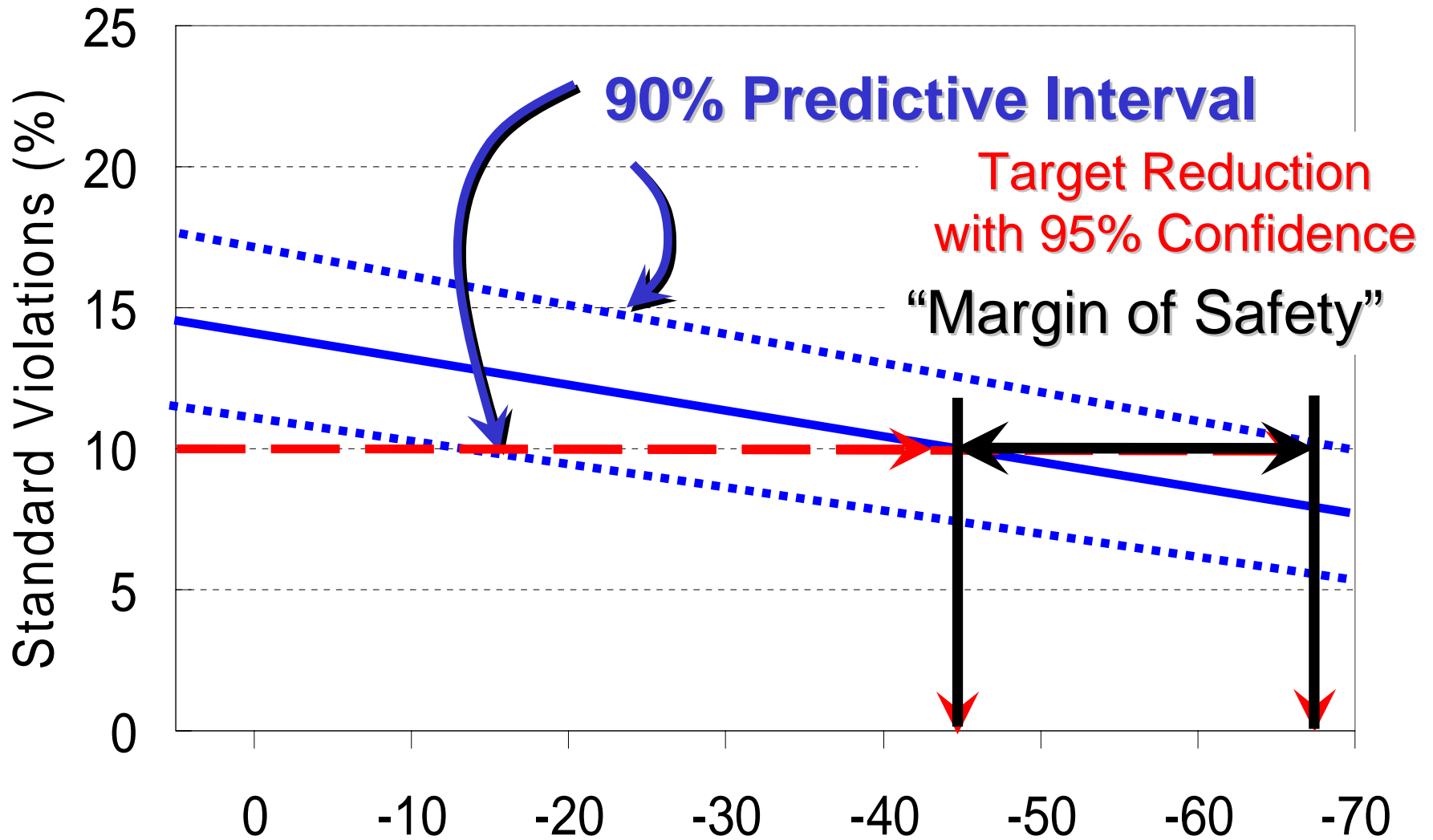


# Project Objectives

- **Develop an adaptive implementation modeling and monitoring strategy (AIMMS) for TMDL improvement.**
- **Apply and evaluate AIMMS on the Neuse Estuary TMDL in North Carolina.**



# N Reductions Relative to 1991-95



**We need predictions to guide  
TMDL decision making, so what  
should we do?**

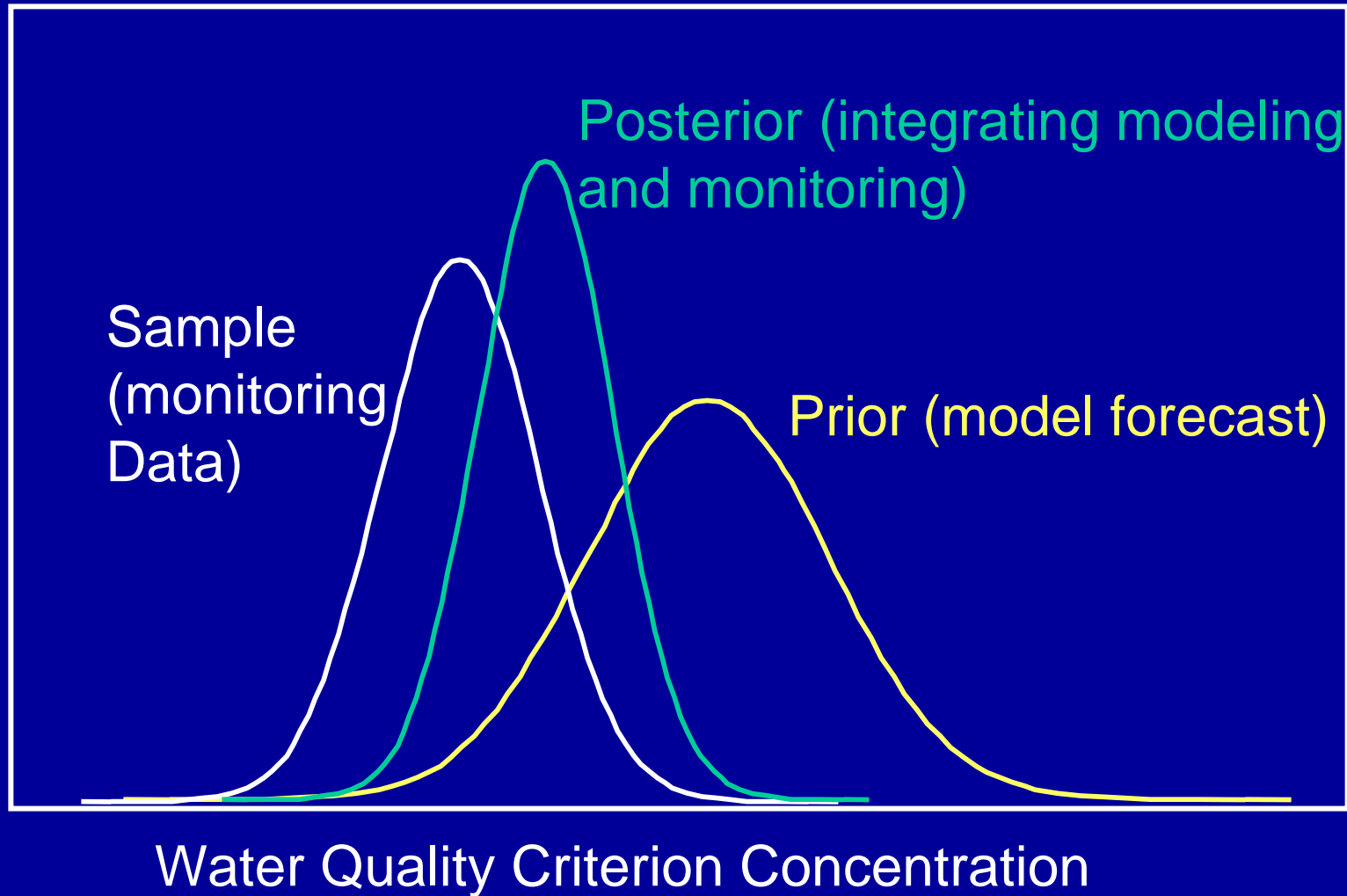
***Adaptive Implementation***

**We can “learn while doing;” that is, we can observe how the real system (the actual waterbody) responds, and then use that information to augment and improve the prediction for the modeled system.**

# How might we conduct adaptive implementation?

- *Step 1:* To define the allowable pollutant load (the TMDL), a water quality model is applied; the forecast from this model provides the initial estimate of how the waterbody will respond to the pollutant load reductions required in the TMDL.
- *Step 2:* After the TMDL is implemented (i.e., nonpoint & point source pollution controls in place), a *properly-designed* monitoring & research program is established; this program can be focused on assessment of particular pollutant controls and/or on overall waterbody compliance with standards.
- *Step 3:* The pre-implementation model forecast (from step 1) is combined with the post-implementation monitoring (from step 2); this provides the best overall estimate of TMDL success and provides the basis for any necessary revisions to the TMDL.

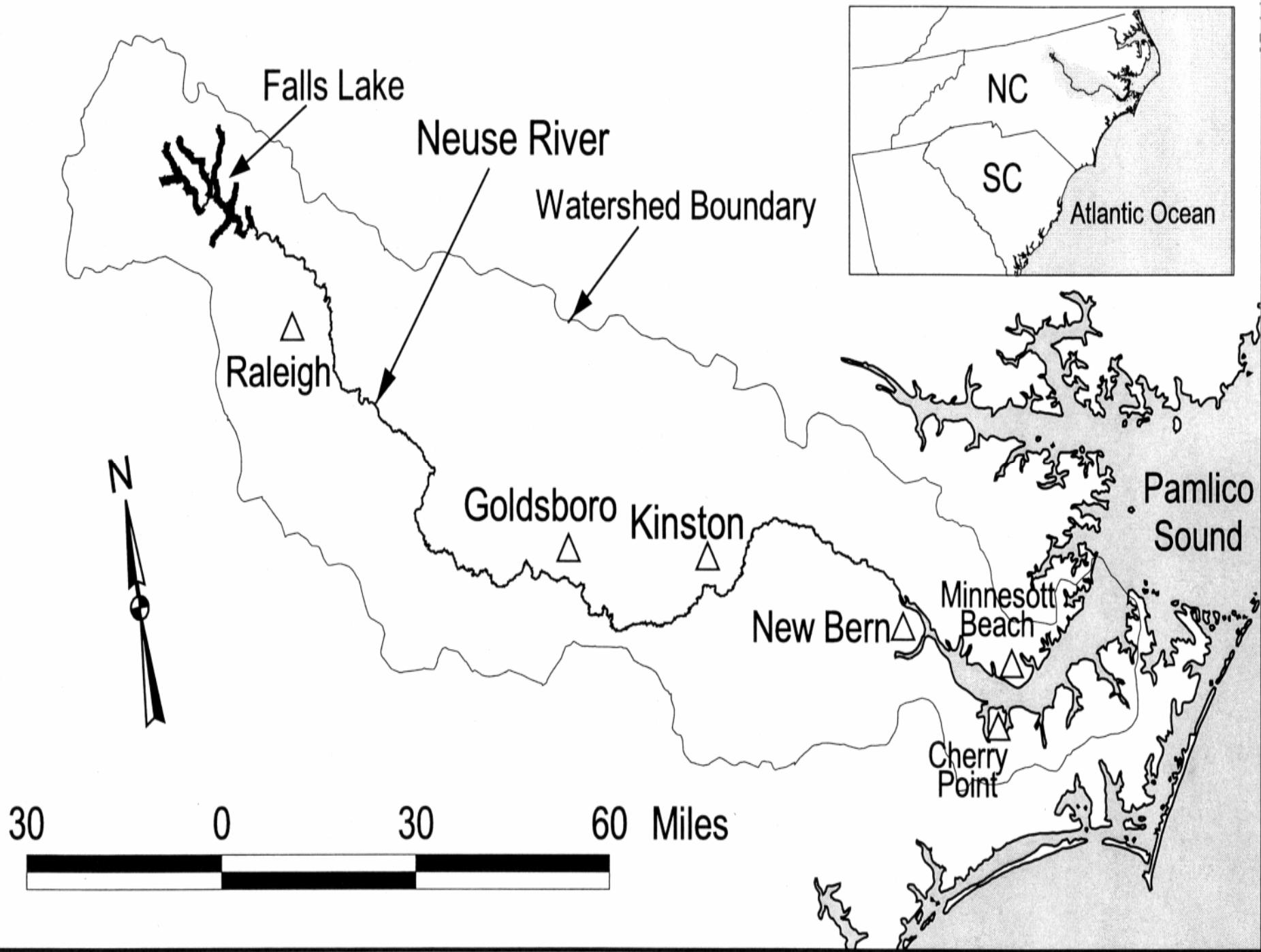
# Adaptive Implementation: Bayesian Analysis





# Example: TN in Neuse Estuary

- Prior distribution of log TN concentration assessed from the Bayesian SPARROW model
- TN monitoring data collected from 1992 – 2000
- The log TN distribution is updated using one year's data at a time to illustrate sequential updating.



# Neuse SPARROW Model

$$\text{TN Load}_i = \sum_{j \in J(i)} \sum_{n=1}^N \beta_n S_{n,j} \exp(-\alpha' Z_j) H^r_{i,j} H^s_{i,j} \epsilon_i$$

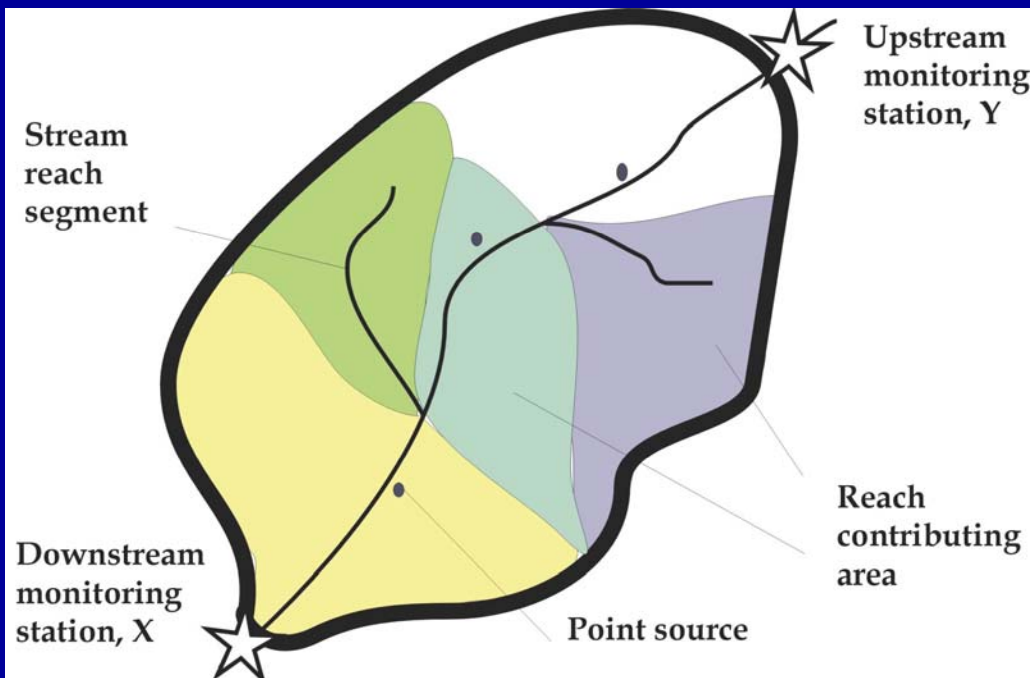
Stream  
Load at  
reach i

Sources

Land-to-water  
transport

Aquatic  
transport

Error



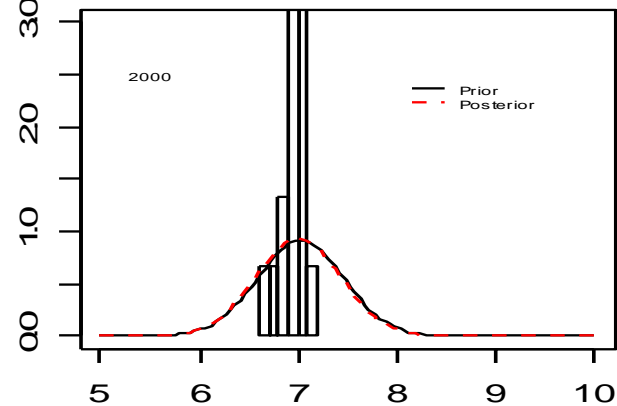
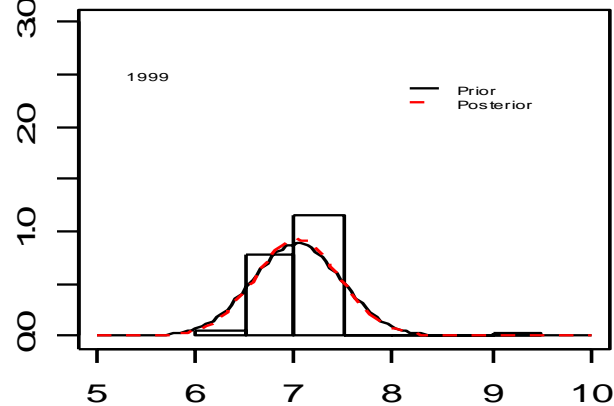
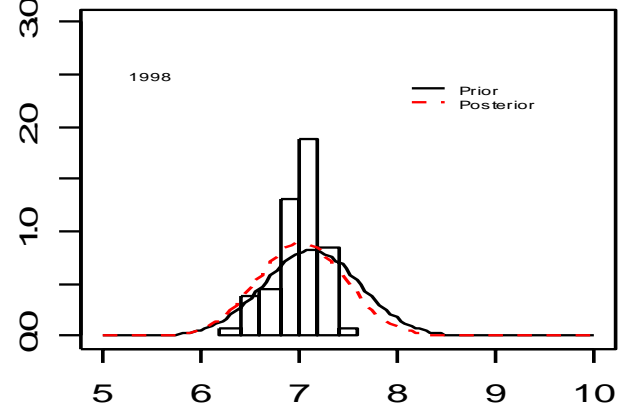
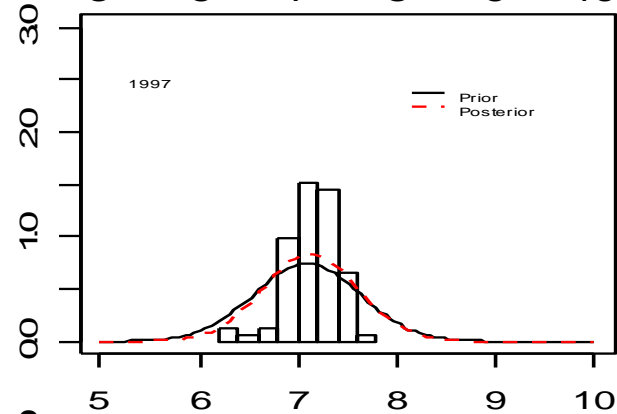
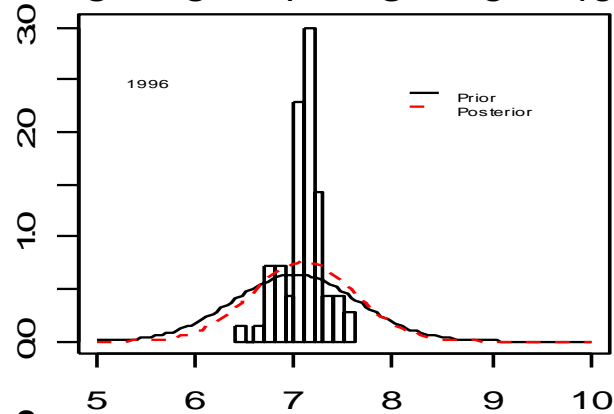
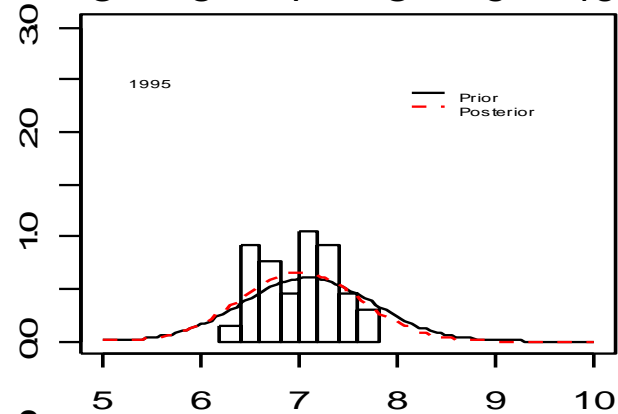
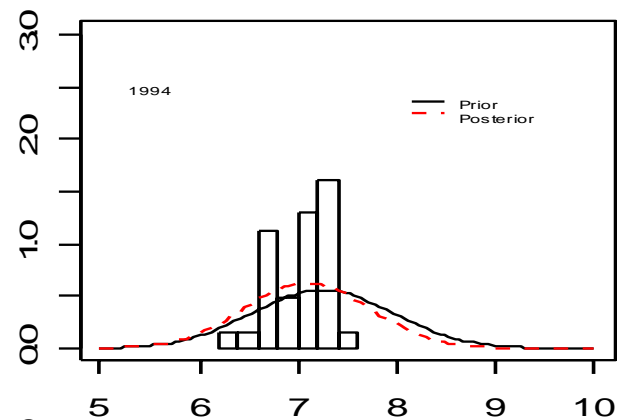
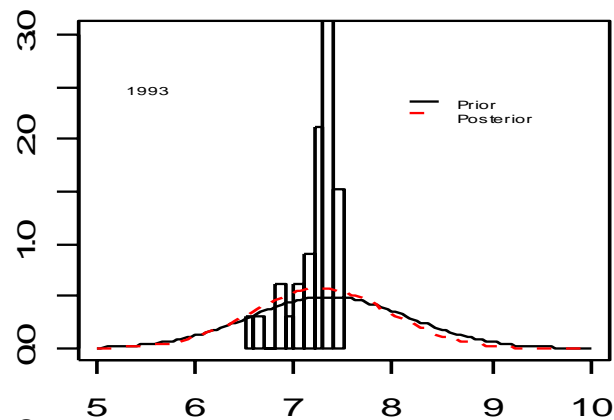
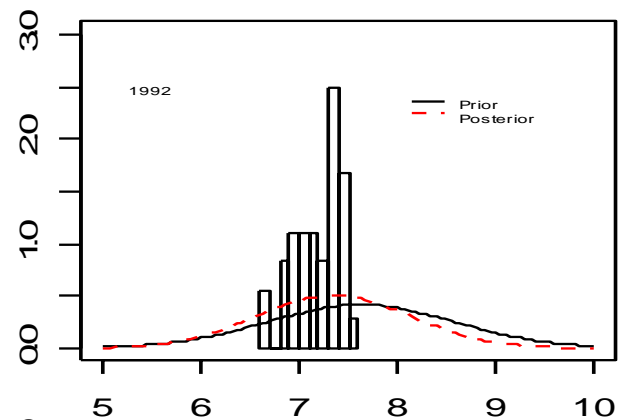
$n$  = number of sources  
 $j$  = reaches in the set  $J(i)$

# Neuse Estuary: Prior Parameters

Using the Bayesian SPARROW model to create the prior distribution, we generated 10,000 pairs of samples of the mean and variance for log TN.

# Sequential Updating

- Repeated use of the Bayes theorem
- Current posterior becomes prior when new data are available.



Log TN Concentration



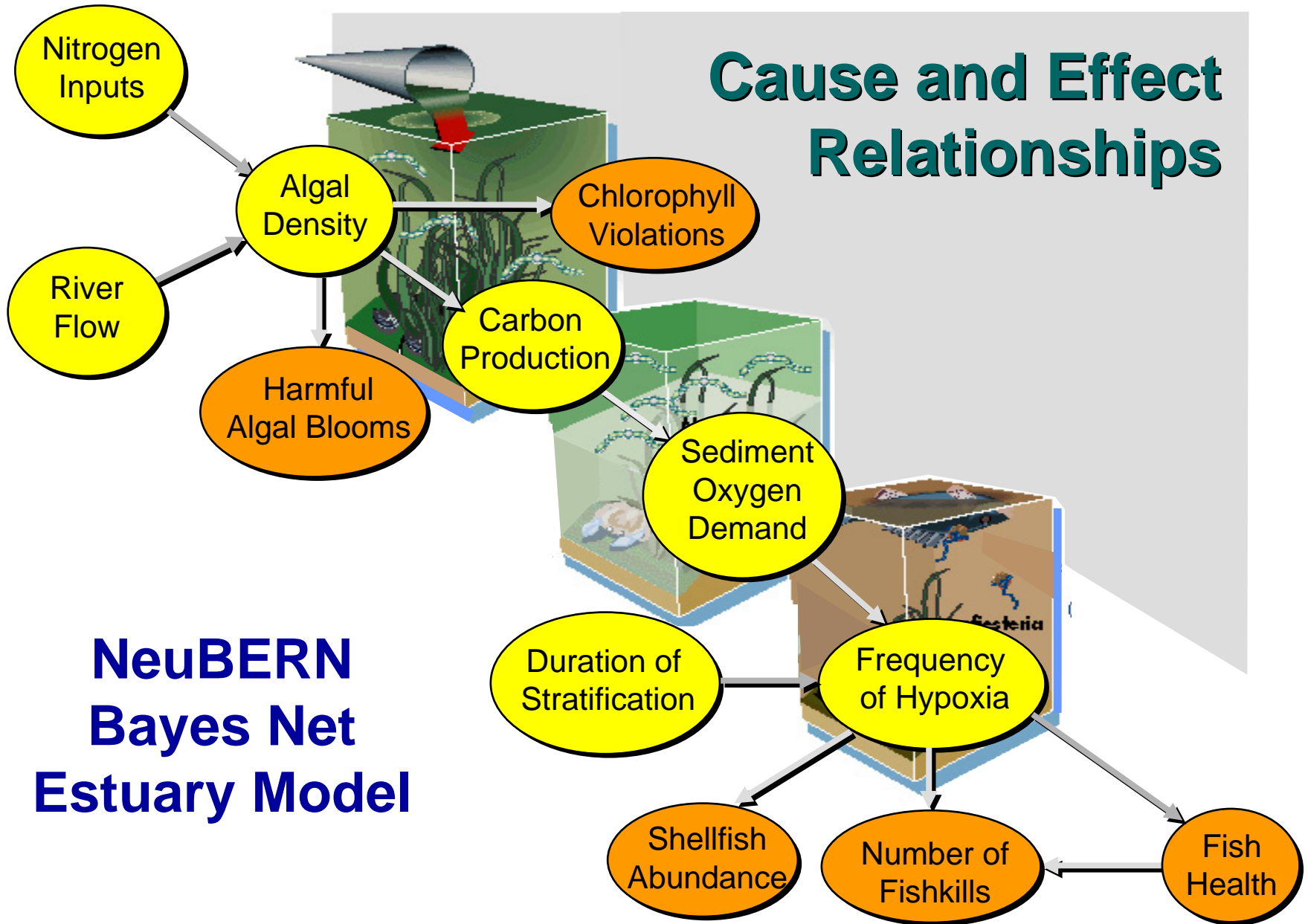
# Example: Chl a in Neuse Estuary

The Chlorophyll model in NeuBERN:

$$\log(chla) = \begin{cases} \beta_1 + \log(\theta)(T - 20) + \beta_2(15.7 - \text{Log}(\text{Flow})) + \beta_4 e^{TN}, & \text{Log}(\text{Flow}) \leq 15.7 \\ \beta_1 + \log(\theta)(T - 20) + \beta_3(\text{Log}(\text{Flow}) - 15.7) + \beta_4 e^{TN}, & \text{Log}(\text{Flow}) > 15.7 \end{cases}$$



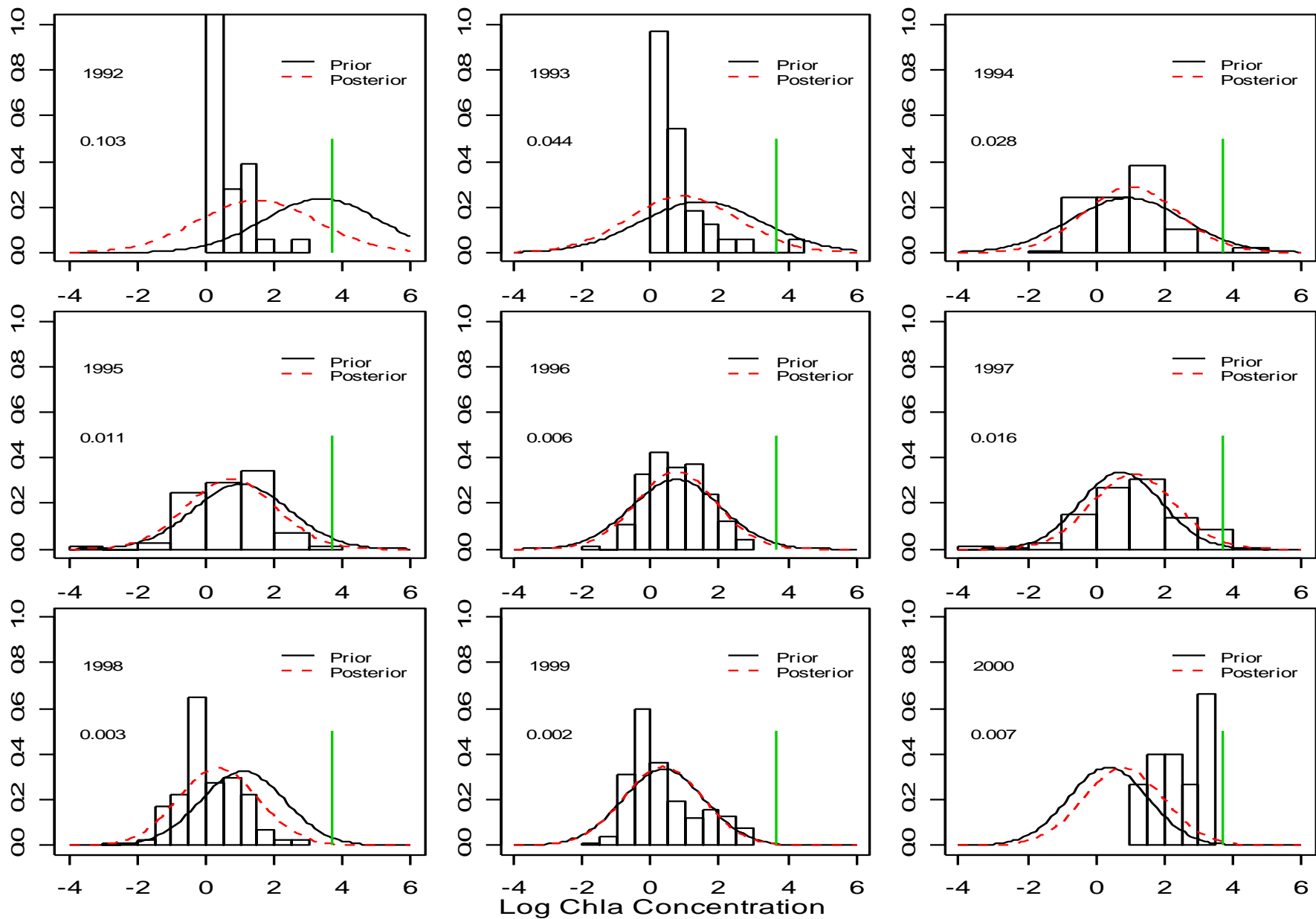
# Cause and Effect Relationships

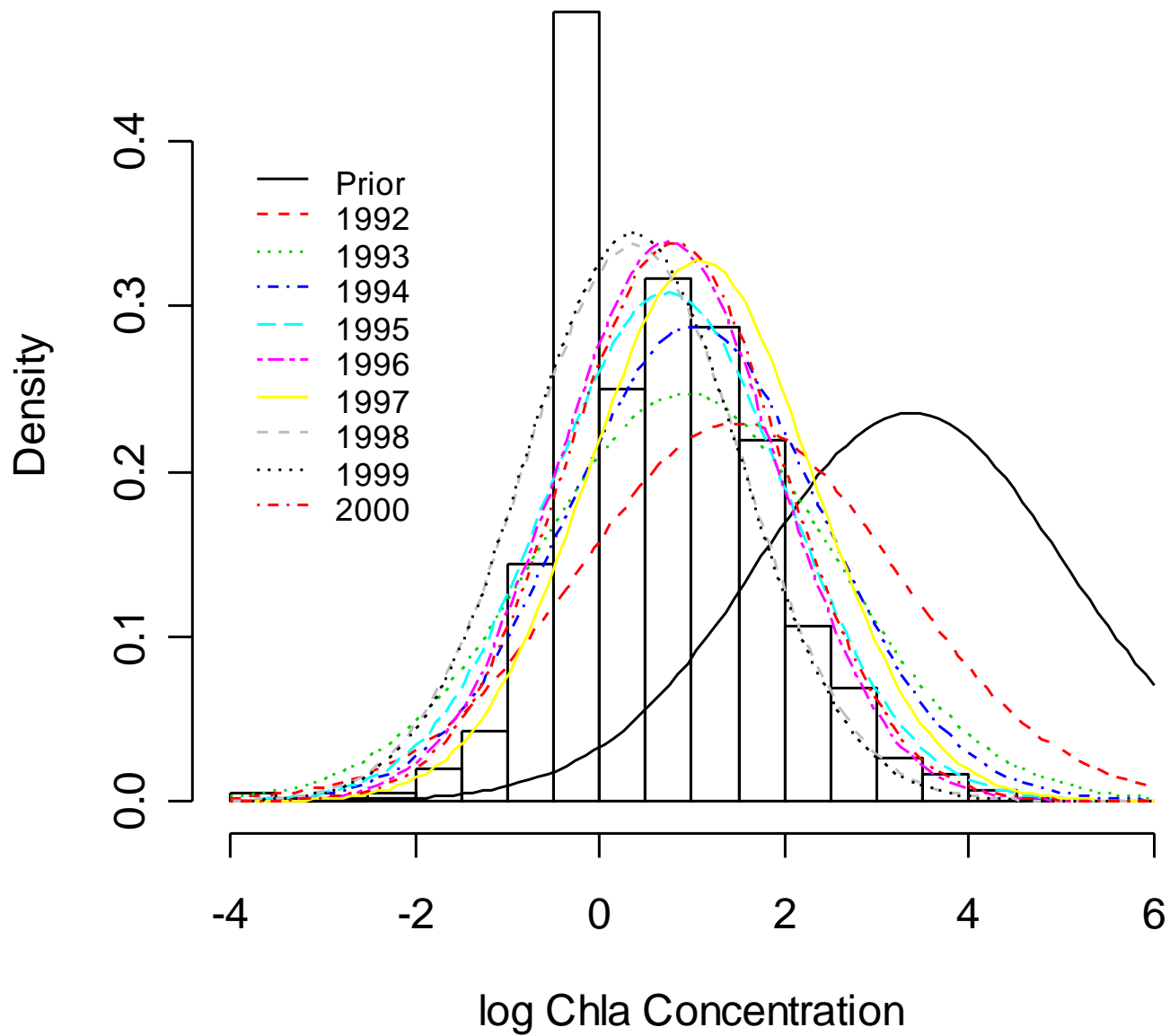


**NeuBERN  
Bayes Net  
Estuary Model**

# Prior Information

- TN: random samples from Bayesian SPARROW
- $\beta$ 's: original NeuBERN regression analysis
- Model error: original regression analysis
- Monte Carlo simulation: random samples of  $\log(chla)$
- Assume  $\log(chla) \sim N(\mu, \sigma^2)$





# Example: Chla Model Updating

- Using yearly data to update model parameters

$$\log(chla) = \begin{cases} \beta_1 + \log(\theta)(T - 20) + \beta_2(Ch - \text{Log}(\text{Flow})) + \beta_4 e^{TN}, & \text{Log}(\text{Flow}) \leq Ch \\ \beta_1 + \log(\theta)(T - 20) + \beta_3(\text{Log}(\text{Flow}) - Ch) + \beta_4 e^{TN}, & \text{Log}(\text{Flow}) > Ch \end{cases}$$

# Example: Chla Model Updating

- Probabilistic expression:

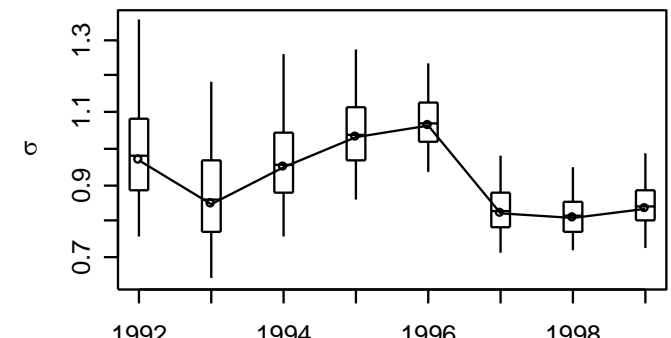
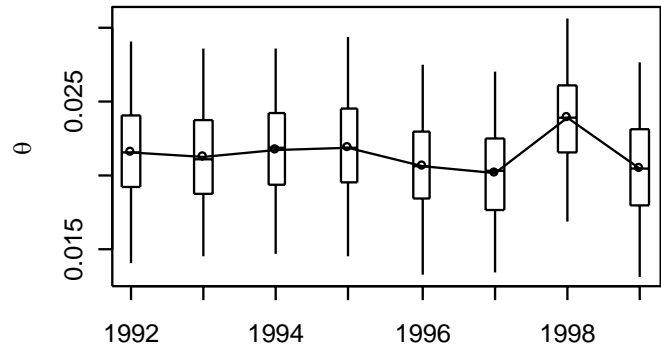
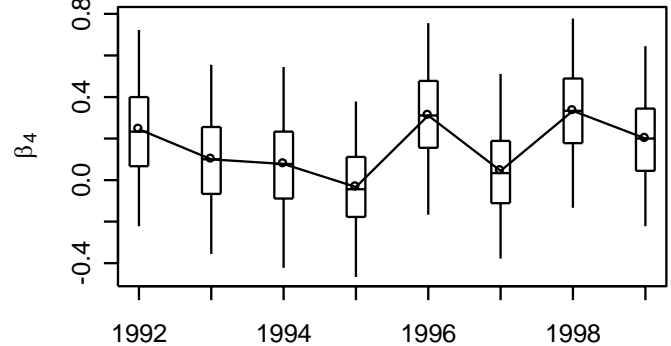
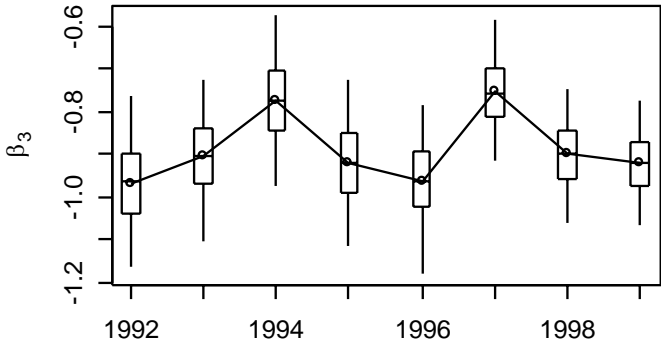
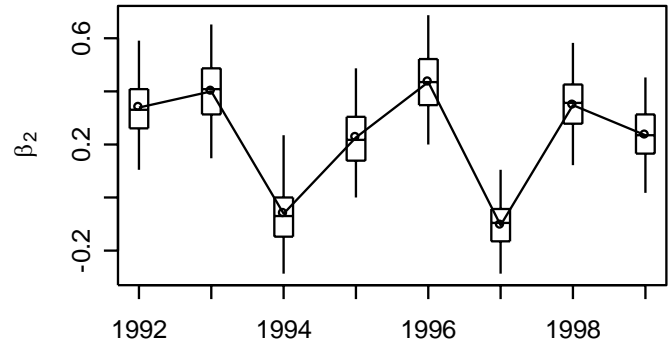
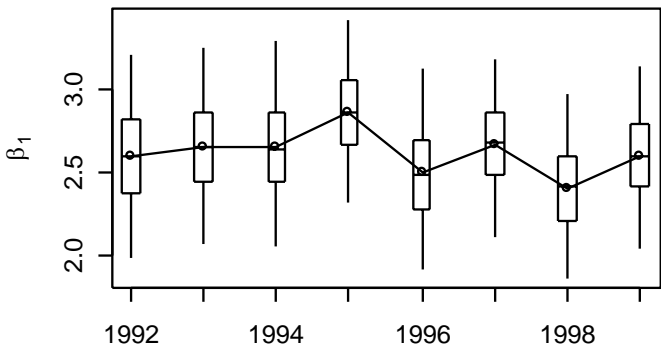
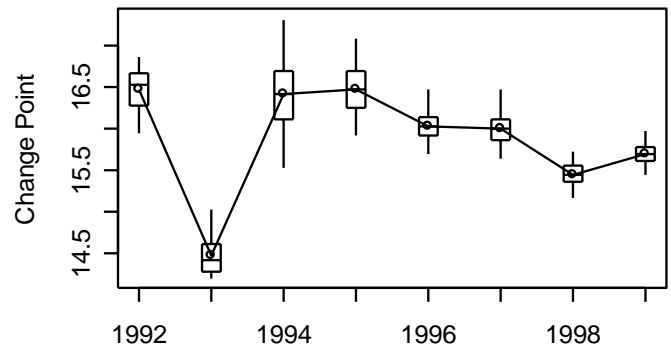
$$\log(\text{Chla}) \sim N(\mu, \sigma^2)$$

Where:  $\mu = f(\beta, \theta, Ch, T, TN)$

Same general setting under Bayes Theorem, but  
with a large number of parameters

# Example: Chla Model Updating

- No conjugate family of priors
- No analytical solutions for posteriors
- Numerical solution using Markov chain Monte Carlo simulation





# Post (TMDL) Implementation Questions

- **Has compliance with the water quality standard been achieved?**
- **If compliance has not been achieved, what pollutant reduction actions did not respond as predicted?**

# Tasks Completed or Underway

- **NeuBERN and SPARROW models have been linked within a Bayesian framework (WinBUGS)**
- **NeuBERN is being re-specified to add more mechanism.**
- **SPARROW has been re-calibrated to address spatial correlation and improve parameter estimators. Ultimately, it will be further revised to allow for subwatershed-specific parameters.**

# Issues to Address in Year 3

- Use the CUAHSI “digital watershed” to efficiently link SPARROW and NeuBERN
- Represent land use (pollutant load) change in SPARROW
- Characterize prior probabilities for SPARROW parameters
- Design monitoring program (sensitivity analysis)
- Assess role of stakeholders

# **Expected Outcomes**

- **Re-assessment of the Neuse nitrogen TMDL for NC Division of Water Quality**
- **Development of guidelines and procedures for adaptive implementation of TMDLs**
- **Determination of effective roles for stakeholders**